

Homework 9 — Prolog — assigned Tuesday 27 April — due Monday 3 May

Extra credit.

9.1 Grammar (30pts)

The following language over the alphabet $\{a, b, c\}$ $L = \{a^n b^n c^n \mid n \in \mathbb{N}\}$ can be generated by the following grammar:

$$G = (\{S, X, Y\}, \{a, b, c\}, S, F),$$

where the productions are:

$$F = \{S \rightarrow abc, S \rightarrow aXbc, Xb \rightarrow bX, Xc \rightarrow Ybcc, bY \rightarrow Yb, aY \rightarrow aaX, aY \rightarrow aa\}$$

This grammar is not context-free, because on the left-hand sides of some productions there are strings longer than single non-terminals. (In fact, there is no context-free grammar for this language.) However, the productions in this grammar satisfy a *length-increasing* property: the number of symbols on the right is never less than the number on the left. Such grammars are called context-sensitive. (Note that there are grammars, and their languages, that are not even context-sensitive.)

Write a Prolog program that determines whether a string belongs to the language L . Strings over the alphabet $\{a, b, c\}$ will be represented as Prolog lists of Prolog atoms `a`, `b`, and `c`. You should split the program into a set of predicates that are general-purpose (for any context-sensitive grammar), and a set of predicates that describe the grammar G .

The program should result in queries like these:

```
?- accepts([ ]).
No
?- accepts([a]).
No
?- accepts([a,b]).
No
?- accepts([a,b,b]).
No
?- accepts([a,b,b,c]).
Yes
?- accepts([a,a,b,b,c,c]).
Yes
?- accepts([a,a,a,a,a,b,b,b,b,b,c,c,c,c,c]).
Yes
```

?- accepts([a,a,a,a,a,a,b,b,b,b,b,b,c,c,c,c,c,c,a]).
No

You may find useful the predefined predicate `length/2`, which works as follows: given a list `X`, the goal `length(X,N)` succeeds and sets `N` to the integer equal to the length of the list `X`.

You should test your program on the queries above and others you find useful to cover the various cases of strings in the language and outside the language. Make sure that your program does not go into an infinite loop on any inputs. Do not submit your program unless it has passed all these tests.

9.2 Tic-tac-toe (20pts)

Write a Prolog program that allows a human user to play tic-tac-toe against the computer. Either the computer or the human can move first. The computer may choose its moves using any policy whatsoever, including random. The first player to move is the X player, the second is the O player.

Suggested representations of a tic-tac-toe board include these possibilities: `[x,o,o,b,x,b,b,b,x]` or `[[x,o,o],[b,x,b],[b,b,x]]`. (`b` stands for an unoccupied square.) Both of these examples are lists intended to represent a winning board for X in which X has conquered the bend (the diagonal from top left to bottom right).

You do not have to worry about interactive input-output. It suffices to write a predicate `computersmove(L1,L2)`, which, when given an instantiated board `L1`, produces a unique board `L2` as the outcome of the computer's move. Assume that the human will repeatedly query this predicate.

Hints: Consider writing a predicate `xwins(L)`, meaning that the board `L` is a winning board for X, and a similar predicate `owins(L)`. Consider writing a predicate `okmove(L1,L2)`, meaning that from the board `L1` it is legal to get to the board `L2` in the very next move.

9.3 Smarter tic-tac-toe (10pts)

Same as above, but the computer should use a policy that guarantees it will not lose if it plays first.

9.4 Mastermind (40pts)

Design and implement the client, the scorer, and the driver of Exercise 8.5 in Prolog. Consider allowing arbitrary atoms, such as `orange`, instead of just numbers as in ML.

9.5 Scheme (50pts)

Design a representation for Scheme values and expressions in Prolog, and write a predicate `evaluatesto/2` which relates a Scheme expression to its value, if any. Carefully choose the Scheme subset you wish to handle—make it as small as possible to keep the exercise manageable. Remember that `lambda` is sufficient, and that without `lambda` you don't have Scheme.

How to turn in

Make sure that you have thoroughly tested your code, and include all your test runs!

Turn in your code by running

`~clint/handin your-file`

on a regular UNM CS machine. You should use whatever filename is appropriate in place of `your-file`.

Include the following statement with your submission, signed and dated:

I pledge my honor that in the preparation of this assignment I have complied with the University of New Mexico Board of Regents' Policy Manual, including Section 4.8, Academic Dishonesty.