

Homework 5 — ML — assigned Thursday 6 April — due Sunday 16 April

5.1 Interpreter (100pts) [A.7; C; E; K.1.1; K.2.2; K.2.3]

5.1.1 General description

Consider a simple stack machine for integer list manipulation. The stack machine has a program p , a program counter pc , a stack s that may hold integers and lists, and a stack top pointer sp . The instructions of the machine and their effect on the stack are described by the following table:

Instruction	Stack before	Stack after	Effect
CST i	$s \Rightarrow$	$i\ s$	Push integer constant i
ADD	$i_2\ i_1\ s \Rightarrow$	$(i_1 + i_2)\ s$	Add integers
SUB	$i_2\ i_1\ s \Rightarrow$	$(i_1 - i_2)\ s$	Subtract integers
DUP	$v\ s \Rightarrow$	$v\ v\ s$	Duplicate
SWAP	$v_2\ v_1\ s \Rightarrow$	$v_1\ v_2\ s$	Swap
POP	$v\ s \Rightarrow$	s	Pop
GOTO a	$s \Rightarrow$	s	Jump to a
IFNZRO a	$i\ s \Rightarrow$	s	Jump to a if $i \neq 0$
CALL a	$v\ s \Rightarrow$	$v\ r\ s$	Call function at a , pushing return address r
RET	$v\ r\ s \Rightarrow$	$v\ s$	Return: jump to r
MKNIL	$s \Rightarrow$	$\text{Nil}\ s$	Push Nil (the empty list)
MKCONS	$t\ i\ s \Rightarrow$	$\text{Cons}(i,t)\ s$	Push cons node
LISTCASE a	$\text{Nil}\ s \Rightarrow$	s	If Nil, do not jump
LISTCASE a	$\text{Cons}(i,t)\ s \Rightarrow$	$t\ i\ s$	If Cons, unpack components and jump to a
PRINT	$v\ s \Rightarrow$	$v\ s$	Print v and keep it
STOP	$s \Rightarrow$	$-$	Halt the machine

In the table, i stands for an integer, a for an address, within the program, r for an address within the program, t for a list, v for an arbitrary value, and s for the remainder of the stack (0 or more values).

An instruction with an argument (CST, GOTO, IFNZRO, CALL, LISTCASE) takes up two positions in the program.

Under any circumstances not covered by the table, the machine will crash. For instance, if the instruction to be executed is an ADD but the top stack element is a list rather than an integer, the machine will crash.

5.1.2 The emulator (interpreter) (60pts)

Given the following elements of a list stack machine interpreter written in ML, complete the rest of the code.

```
datatype bytecode = B_CST
                  | B_ADD
                  | B_SUB
                  | B_DUP
```

```

        | B_SWAP
        | B_POP
        | B_GOTO
        | B_IFNZRO
        | B_CALL
        | B_RET
        | B_MKNIL
        | B_MKCONS
        | B_LISTCASE
        | B_PRINT
        | B_STOP
        | B_INT of int
        | B_ADDR of int

type program = bytecode Vector.vector

datatype list' = Nil
               | Cons of int * list'

datatype object = (**** part A of your code here ****)

type stack = (**** part B of your code here ****)

fun listToString Nil = "Nil"
  | listToString (Cons (i, l)) =
    "Cons(" ^ Int.toString i ^ ", " ^ listToString l ^ ")"

fun objectToString (Integer i) = Int.toString i
  | objectToString (List l) = listToString l

fun execcode (p: program) (s: stack, pc: int)
  : stack * int =
  let
    fun step (s: stack, pc: int): (stack * int) option =
      case Vector.sub (p, pc) of
        B_CST => (case Vector.sub (p, pc+1) of B_INT i =>
          SOME (Integer i :: s, pc+2))
        | B_ADD => (case s of (Integer i2)::(Integer i1)::s' =>
          SOME (Integer (i1+i2) :: s', pc+1))
  in
    (**** part C (the main part) of your code here ****)

    fun loop spc =

```

```

        let
            val next = step spc
        in
            case next of
                NONE => spc
              | SOME spc' => loop spc'
            end
        in
            loop (s, pc)
        end

fun exec p = execcode p ([], 0)

(* an example: *)
val program = Vector.fromList [B_CST, B_INT 1, B_CST,
                              B_INT 1, B_SUB, B_MKNIL,
                              B_MKCONS, B_PRINT, B_STOP]

val xxx = exec program;

(* under SML/NJ, the following is printed:
Cons(0, Nil)
val program =
  #[B_CST,B_INT 1,B_CST,B_INT 1,B_SUB,B_MKNIL,B_MKCONS,B_PRINT,B_STOP]
  : bytecode vector
val xxx = ([List (Cons (#,#))],8) : stack * int
*)

```

Place the code inside a structure `ListStackMachine`. (In the example above, the code was not yet placed in a structure.)

5.1.3 Analysis and discussion (40pts)

Having implemented the interpreter, answer the following questions.

1. (5pts) Manually execute the code below on the stack machine. Show the stack contents after every instruction and show what is printed on the console:

```

0: CST 100
2: CST 11
4: ADD
5: MKNIL
6: MKCONS
7: PRINT
8: STOP

```

2. (5pts) Write stack machine code to create and print the list `Cons(111, Cons(222, Nil))`.
3. (5pts) The instructions `CALL` and `RET` can be used to implement simple functions. What does the following stack machine program do, assuming that the integer 42 is on the stack top when execution is started at instruction address 0?

```

0: CALL 4
2: PRINT
3: STOP
4: DUP
5: DUP
6: MKNIL
7: MKCONS
8: MKCONS
9: MKCONS
10: RET

```

Show the contents of the stack after each instruction, in the order in which the instructions are executed.

4. (5pts) Write a stack machine program that, given that integer $n \geq 0$ is on the stack top, builds and prints an n -element list of the form `Cons(n, Cons(n-1, ..., Cons(1, Nil), ...))`. Provide both an iterative and a recursive solution.
5. (5pts) The instruction `LISTCASE` can be used to test whether the list on the stack top is `Nil` or a `Cons`. If the stack top element is `Nil`, execution simply continues with the next instruction. If the stack top element is `Cons(i, t)`, then the integer i and the list tail t are unpacked on the stack and execution continues at address a .

Consider the following stack machine code fragment:

```

21: LISTCASE 27
23: CST 999
25: GOTO 28
27: POP
28: PRINT

```

Assume that the list `Cons(111, Cons(222, Nil))` is on the stack top when the function at address 21 is called (by `CALL 21`). What is on the stack top, and is therefore printed, when control reaches instruction 28? What is printed if the empty list is on the stack top when `CALL 21` is executed?

6. (5pts) Write a stack machine function that, given that a list is on the stack top, computes the sum of the list elements. Provide both an iterative and a recursive solution.
7. (10pts) Write an ML function

```
mklist: int -> bytecode Vector.vector
```

which, for a given integer $n \geq 0$ generates stack machine code which, if executed starting with an initial program counter of 0 and an empty initial stack, will build and print a list of n Cons nodes of the form:

```
Cons(2n, Cons(2n - 2, ..., Cons(2, Nil) ...))
```

5.2 Graduate credit (50pts)

This problem is required for graduate credit; other course participants may solve this problem for extra credit.

This exercise is similar to homework exercise 4.2. The goal is to translate an expression (given by the data type from homework exercise 3.5) into a program for the stack machine from the above exercise 5.1.

Unlike the C program from exercise 4.2, the stack machine is not capable of querying the user for the values of the free variables. Instead, the stack machine program will expect to find the values of the free variables on its stack. They will be in alphabetical order, such that the lexicographically lowest variable's value is at the bottom of the stack.

As in exercise 4.2, any subexpression that can be evaluated independent of the values of free variables must be evaluated by the translator, not by the stack machine program. To make this more precise: if and only if the arguments to an operator do not depend on any free variables, we consider that the result of the operator does not depend on any free variables. (This means that we do not use algebraic knowledge to simplify, e.g., $x - x$ to 0.)

Place the declarations from exercise 3.5 into a structure `ArithmeticExpression`. Write a structure `Translator` :> `TRANSLATOR` where the signature `TRANSLATOR` is as follows:

```
signature TRANSLATOR =
  sig
    val translate: ArithmeticExpression.expr -> ListStackMachine.program
  end
```

The initial program counter value must be 0; other than that, there are no restrictions on the shape of the stack machine code produced by the translator.

How to turn in

Submission instructions have been posted to the course mailing list.

Include the following statement with your submission, signed and dated:

I pledge my honor that in the preparation of this assignment I have complied with the University of New Mexico Board of Regents' Policy Manual.